

From the spherical-mirror equation or the thin-lens equation, $\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}$, we have

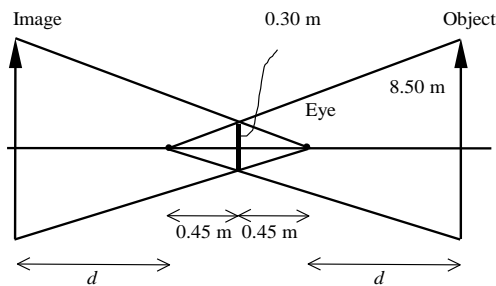
$$\frac{1}{d_i} = \frac{1}{f} - \frac{1}{d_o} = \frac{d_o - f}{d_o f}. \quad \text{Or} \quad d_i = \frac{d_o f}{d_o - f}. \quad \text{This is used in the solutions of many exercises.}$$

1. (b).
2. (b).
3. (c).
4. It is **infinite, because it cannot focus light to a point**.

9. (a) Image distance equals object distance. The distance from object to image is $2.0 \text{ m} + 2.0 \text{ m} = \mathbf{4.0 \text{ m}}$.
- (b) **Upright, virtual, and same size**.

$$12. \quad A = a^2, \quad a = \sqrt{A} = \sqrt{900 \text{ cm}^2} = 30 \text{ cm} = 0.30 \text{ m}.$$

Use similar triangles. $\frac{d + 0.45 \text{ m} + 0.45 \text{ m}}{8.50 \text{ m}} = \frac{0.45 \text{ m}}{0.30 \text{ m}}, \quad d = \mathbf{12 \text{ m}}$.



13. (a) Image distance equals object distance, and so it is **1.5 m behind the mirror**.
- (b) The image also moves at 0.5 m/s toward the dog, and so the relative velocity of the dog to the image is $0.5 \text{ m/s} + 0.5 \text{ m/s} = \mathbf{1.0 \text{ m/s}}$.
16. (a) The mirror needs to be half as tall as the object as explained in Example 23.7. So it is **0.85 m** tall.
- (b) It is independent of object distance, and it is still **0.85 m**.
19. (d).
20. (a).
21. (a) concave. A shaving mirror forms larger images than object. Plane and convex mirrors cannot form larger images.
22. (a) The plane mirror gives a large view of the area immediately around that side of the truck. The small convex mirror gives a wide-angle perspective of the road in back of both sides of the truck (but the image is smaller).
- (b) These are convex mirrors that give a better field of view, but also images are smaller than objects (so the image distances are smaller than object distances) and hence appear closer than they actually are.
- (c) Yes, it can be considered as a converging mirror, because it collects a large amount of radio waves and focuses them onto a small area.

$$\mathbf{28.} \quad d_o = 20 \text{ cm}, \quad f = \frac{R}{2} = \frac{30 \text{ cm}}{2} = 15 \text{ cm}, \quad d_i = \frac{d_o f}{d_o - f} = \frac{(20 \text{ cm})(15 \text{ cm})}{20 \text{ cm} - 15 \text{ cm}} = \mathbf{60 \text{ cm}}.$$

$$M = -\frac{d_i}{d_o} = -\frac{60 \text{ cm}}{20 \text{ cm}} = -3.0. \quad \text{So} \quad h_i = M h_o = -3.0 (3.0 \text{ cm}) = -9.0 \text{ cm}. \quad \text{It is } \mathbf{9.0 \text{ cm}} \text{ tall.}$$

$$29. \quad d_i = \frac{(10 \text{ cm})(15 \text{ cm})}{10 \text{ cm} - 15 \text{ cm}} = \mathbf{-30 \text{ cm}}. \quad M = -\frac{-30 \text{ cm}}{10 \text{ cm}} = +3.0.$$

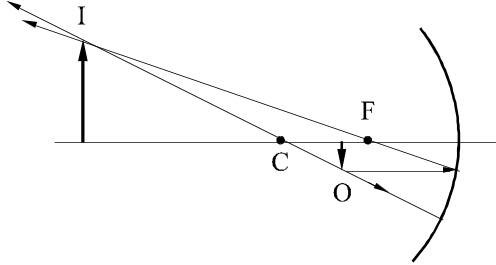
$$\text{So} \quad h_i = +3.0 (1.5 \text{ cm}) = \mathbf{9.0 \text{ cm; virtual, upright, and magnified}}.$$

$$30. \quad (a) \quad d_o = 5.0 \text{ cm}, \quad d_i = -10 \text{ cm (virtual image)}. \quad \frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{5.0 \text{ cm}} + \frac{1}{-10 \text{ cm}} = \frac{1}{10 \text{ cm}},$$

so $f = \boxed{10 \text{ cm}}$, and $R = 2f = \boxed{20 \text{ cm}}$.

(b) $M = -\frac{d_i}{d_o} = -\frac{-10 \text{ cm}}{5.0 \text{ cm}} = +2$ So $h_i = Mh_o = +2 (1.5 \text{ cm}) = \boxed{3.0 \text{ cm}}$.

45. (a) See diagram below.



(b) $f = \frac{R}{2} = \frac{30 \text{ cm}}{2} = 15 \text{ cm}$, $d_o = 20 \text{ cm}$. $d_i = \frac{d_o f}{d_o - f} = \frac{(20 \text{ cm})(15 \text{ cm})}{20 \text{ cm} - 15 \text{ cm}} = \boxed{60 \text{ cm}}$.

$M = -\frac{d_i}{d_o} = -\frac{60 \text{ cm}}{20 \text{ cm}} = \boxed{-3.0, \text{ real and inverted}}$.

50. $d_i = \frac{d_o f}{d_o - f}$. For concave, $M = -\frac{d_i}{d_o} = \frac{f}{f - d_o} = +1.8$, $f = \frac{9}{4} d_o$.

For convex, we replace f with $-|f| = -f$.

So $M = \frac{f}{f + d_o} = \frac{9/4 d_o}{9/4 d_o + d_o} = \frac{9}{13} = \boxed{0.69}$.

53. **Yes**, it is possible. One is a real image, and the other is a virtual image.

$f = \frac{R}{2} = \frac{40 \text{ cm}}{2} = 20 \text{ cm}$, $M = \pm 3.0$, the + is for a virtual image, and the - is for a real image.

$d_i = -M d_o = \mp 3.0 d_o$. $\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i}$, so $\frac{1}{20 \text{ cm}} = \frac{1}{d_o} + \frac{1}{\mp 3.0 d_o}$,

or $\frac{3 \mp 1}{3 d_o} = \frac{1}{20 \text{ cm}}$. Solving, $d_o = \frac{20 \text{ cm}}{3} (3 \mp 1) = \boxed{13 \text{ cm or } 27 \text{ cm}}$.

54. (c).

55. (d).

56. (d).

57. When the fish is inside the focal point, the image is upright, virtual, and magnified.

58. **Yes**. If the object is inside the focal point ($d_o < f$), the image of a real object is virtual, upright, and magnified.

59. You can **locate the image of a distant object**. The distance from the converging lens to the image is the focal length. **No**, the same method won't work for a diverging lens because a diverging lens does not form real images of real objects.

60. The object distance should be between the focal length and twice the focal length, i.e., $\boxed{2f > d_o > f}$. In this region, the image is real, inverted, and magnified.

67. (a) $f = 12 \text{ cm}$, $M = -2.0$ (real). $d_i = -M d_o = 2.0 d_o$.

$\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{d_o} + \frac{1}{2.0 d_o} = \frac{3}{2 d_o}$, $d_o = \frac{3}{2} f = \frac{3}{2} (12 \text{ cm}) = \boxed{18 \text{ cm}}$.

(b) $M = +2.0$ (virtual). $d_i = -M d_o = -2.0 d_o$.

$\frac{1}{f} = \frac{1}{d_o} + \frac{1}{-2.0 d_o} = \frac{1}{2 d_o}$, $d_o = \frac{1}{2} f = \frac{1}{2} (12 \text{ cm}) = \boxed{6.0 \text{ cm}}$.

77. (a) $d_o = 30 \text{ cm}$, $f = -45 \text{ cm}$. $d_i = \frac{d_o f}{d_o - f} = \frac{(30 \text{ cm})(-45 \text{ cm})}{30 \text{ cm} - (-45 \text{ cm})} = \boxed{-18 \text{ cm}}$.

$$(b) d_i = \frac{(30 \text{ cm})(57 \text{ cm})}{30 \text{ cm} - 57 \text{ cm}} = \boxed{-63 \text{ cm}}.$$

$$\boxed{82}. \quad \text{For } L_1, \quad d_{i1} = \frac{d_{o1} f_o}{d_{o1} - f_o} = \frac{(50 \text{ cm})(30 \text{ cm})}{50 \text{ cm} - 30 \text{ cm}} = 75 \text{ cm}.$$

$$M_1 = -\frac{d_{i1}}{d_{o1}} = -\frac{75 \text{ cm}}{50 \text{ cm}} = -1.5. \quad \text{The image by } L_1 \text{ is the object for } L_2.$$

For L_2 , $d_{o2} = d - d_{i1} = 60 \text{ cm} - 75 \text{ cm} = -15 \text{ cm}$, where d is the distance between the lenses. A negative object means that the "object" is on the image side.

$$d_{i2} = \frac{d_{o2} f_2}{d_{o2} - f_2} = \frac{(-15 \text{ cm})(20 \text{ cm})}{-15 \text{ cm} - 20 \text{ cm}} = \boxed{8.6 \text{ cm}}. \quad M_2 = -\frac{d_{i2}}{d_{o2}} = -\frac{8.57 \text{ cm}}{-15 \text{ cm}} = 0.57.$$

$$\text{So } M_{\text{total}} = M_1 M_2 = (-1.5)(0.57) = -0.86 = \boxed{0.86; \text{ real and inverted}}.$$

85. (b).

86. (b).

87. (b). It cannot focus light or the focal length is at infinity.

88. $\boxed{+, +; +, \infty; +, -; -, -; \infty, -; +, -}$.

$$95. \quad P = \frac{1}{f} = (n - 1) \left(\frac{1}{R_1} + \frac{1}{R_2} \right) = (1.35 - 1) \left(\frac{1}{\infty} + \frac{1}{-0.50 \text{ m}} \right) = \boxed{-0.70 \text{ D}}.$$

$$103. \quad \text{For the first lens, } d_{o1} = 15 \text{ cm}, \quad f_1 = 10 \text{ cm}. \quad d_{i1} = \frac{d_{o1} f_1}{d_{o1} - f_1} = \frac{(15 \text{ cm})(10 \text{ cm})}{15 \text{ cm} - 10 \text{ cm}} = 30 \text{ cm}.$$

$$M_1 = -\frac{d_{i1}}{d_{o1}} = -\frac{30 \text{ cm}}{15 \text{ cm}} = -2.0. \quad \text{The image of the first lens is the object for the second lens.}$$

For the second lens, $d_{o2} = d - d_{i1} = 60 \text{ cm} - 30 \text{ cm} = 30 \text{ cm}$, where d is the distance between the lenses.

$$d_{i2} = \frac{d_{o2} f_2}{d_{o2} - f_2} = \frac{(30 \text{ cm})(20 \text{ cm})}{30 \text{ cm} - 20 \text{ cm}} = \boxed{60 \text{ cm to right of second lens}}.$$

$$M_2 = -\frac{d_{i2}}{d_{o2}} = -\frac{60 \text{ cm}}{30 \text{ cm}} = -2.0. \quad M_{\text{total}} = M_1 M_2 = (-2.0)(-2.0) = \boxed{4.0, \text{ real and upright}}.$$