

33. The ground speed is the magnitude of the horizontal component of velocity.

$$v_g = (120 \text{ mi/h}) \cos 20^\circ = \boxed{113 \text{ mi/h}}.$$

36. (a) $A = \sqrt{A_x^2 + A_y^2}$ and $\theta = \tan^{-1}\left(\frac{A_y}{A_x}\right)$. If A_x and A_y doubles,

$$A' = \sqrt{(2A_x)^2 + (2A_y)^2} = \sqrt{4(A_x)^2 + 4(A_y)^2} = 2\sqrt{A_x^2 + A_y^2} = 2A,$$

$$\theta' = \tan^{-1}\left(\frac{2A_y}{2A_x}\right) = \tan^{-1}\left(\frac{A_y}{A_x}\right) = \theta.$$

So the answer is $\boxed{(1) \text{ vector's magnitude doubles, but direction remains unchanged}}.$

(b) The magnitude triples, but the direction remains unchanged. So it is $\boxed{30 \text{ m at } 45^\circ}$.

40. $A_x = 5.0 \text{ m/s},$ $A_y = 0.$

$$B_x = (10 \text{ m/s}) \cos 60^\circ = 5.0 \text{ m/s}, \quad B_y = (10.0 \text{ m/s}) \sin 60^\circ = 8.66 \text{ m/s}.$$

$$C_x = -(15 \text{ m/s}) \cos 30^\circ = -13.0 \text{ m/s}, \quad C_y = (15 \text{ m/s}) \sin 30^\circ = 7.5 \text{ m/s}.$$

$$(A + B + C)_x = 5.0 \text{ m/s} + 5.0 \text{ m/s} + (-13.0 \text{ m/s}) = -3.0 \text{ m/s},$$

$$(A + B + C)_y = 0 + 8.66 \text{ m/s} + 7.5 \text{ m/s} = 16 \text{ m/s}.$$

$$A + B + C = \sqrt{(-3.0 \text{ m/s})^2 + (16 \text{ m/s})^2} = \boxed{16 \text{ m/s}},$$

$$\theta = \tan^{-1}\left(\frac{16 \text{ m/s}}{3.0 \text{ m/s}}\right) = \boxed{79^\circ \text{ above the } -x\text{-axis}}.$$

41. From Exercise 3.40:

$$(A - B - C)_x = 5.0 \text{ m/s} - 5.0 \text{ m/s} - (-13.0 \text{ m/s}) = 13 \text{ m/s},$$

$$(A - B - C)_y = 0 - 8.66 \text{ m/s} - 7.5 \text{ m/s} = -16 \text{ m/s}.$$

$$\text{So } A - B - C = \sqrt{(13 \text{ m/s})^2 + (-16 \text{ m/s})^2} = \boxed{21 \text{ m/s}},$$

$$\theta = \tan^{-1}\left(\frac{16 \text{ m/s}}{13 \text{ m/s}}\right) = \boxed{51^\circ \text{ below the } +x\text{-axis}}$$

52. (a) Since $F_{2x} = F_{1x}$, or $F_2 \cos 45^\circ = F_1 \cos 45^\circ$. The answer is $\boxed{(2) F_2 = F_1}$.

$$(b) F_{1y} + F_{2y} = F_1 \sin 45^\circ + F_2 \sin 45^\circ = 2F_1 \sin 45^\circ = 2(100 \text{ N}) \sin 45^\circ = 141 \text{ N}.$$

$$\Sigma F_y = 141 \text{ N} - 100 \text{ N} - F_3 = 0. \text{ So } F_3 = \boxed{41 \text{ N down}}$$

53. (a) $(10.5 \text{ m}) \cos 45^\circ = 7.42 \text{ m},$ $(10.5 \text{ m}) \cos 40^\circ = 8.04 \text{ m},$ $(10.5 \text{ m}) \sin 40^\circ = 6.75 \text{ m}.$

The desired displacement is $\vec{d} = (-7.42 \text{ m}) \hat{x} + (7.42 \text{ m}) \hat{y}$.

The first shot is $\vec{d}_1 = (-6.75 \text{ m}) \hat{x} + (8.04 \text{ m}) \hat{y}$.

The second shot should be $\vec{d}_2 = \vec{d} - \vec{d}_1 = (-0.67 \text{ m}) \hat{x} + (-0.62 \text{ m}) \hat{y}$.

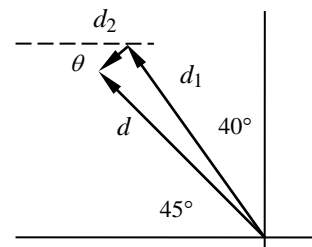
$$\theta = \tan^{-1}\left(\frac{0.62}{0.67}\right) = \boxed{42.8^\circ \text{ south of west}}$$

$$(b) d_2 = \sqrt{(-0.67 \text{ m})^2 + (-0.62 \text{ m})^2} = \boxed{0.91 \text{ m}}.$$

(c) The reason is due to the fact that the ball $\boxed{\text{might travel in a curve}}$.

62. Given: $v_{x0} = 1.5 \times 10^6 \text{ m/s},$ $v_{y0} = 0,$ $x = 0.35 \text{ m}.$ Find: $y.$ (Take both x_0 and y_0 as 0.)

First find the time of flight from the horizontal motion.



$$x = x_o + v_{xo} t, \quad \Rightarrow \quad t = \frac{x}{v_{xo}} = \frac{0.35 \text{ m}}{1.5 \times 10^6 \text{ m/s}} = 2.33 \times 10^{-7} \text{ s.}$$

$$y = y_o + v_{yo} t - \frac{1}{2} g t^2 = 0 + 0 - (4.9 \text{ m/s}^2)(2.33 \times 10^{-7} \text{ s})^2 = -2.7 \times 10^{-13} \text{ m.}$$

So it falls $\boxed{2.7 \times 10^{-13} \text{ m}}$. This is a very small distance. Therefore the answer is $\boxed{\text{no}}$, the designer need not worry about gravitational effects.

67. (a) $\boxed{(2) \text{ Ball B collides with ball A}}$ because they have the same horizontal velocity.

$$(b) y = y_o + v_{yo} t - \frac{1}{2} g t^2 = 0 - \frac{1}{2} g t^2, \quad \Rightarrow \quad t = \sqrt{-\frac{2y}{g}} = \sqrt{-\frac{2(-1.00 \text{ m})}{9.80 \text{ m/s}^2}} = 0.452 \text{ s. (Take } y_o \text{ as 0.)}$$

$$x = x_o + v_{xo} t = 0 + (0.25 \text{ m/s})(0.452 \text{ s}) = \boxed{0.11 \text{ m}} \text{ for both. (Take both } x_o \text{ as 0.)}$$

70. $v_{xo} = v_o \cos \theta = (15.0 \text{ m/s}) \cos 15.0^\circ = 14.5 \text{ m/s,}$

$$v_{yo} = v_o \sin \theta = (15.0 \text{ m/s}) \sin 15.0^\circ = 3.88 \text{ m/s.}$$

(Take both x_o and y_o as 0.)

$$(a) \text{ At maximum height, } v_y = 0. \quad v_y^2 = v_{yo}^2 - 2g(y - y_o), \quad \Rightarrow \quad y = \frac{(3.88 \text{ m/s})^2}{2(9.80 \text{ m/s}^2)} = \boxed{0.768 \text{ m}}.$$

$$(b) \text{ At impact, } y = 0. \quad y = y_o + v_{yo} t - \frac{1}{2} g t^2, \quad \Rightarrow \quad t = \frac{5.176 \text{ m/s}}{\frac{1}{2}(9.80 \text{ m/s}^2)} = 0.792 \text{ s.}$$

$$\text{So } R = x = x_o + v_{xo} t = 0 + (14.5 \text{ m/s})(0.792 \text{ s}) = \boxed{11.5 \text{ m}}.$$

(c) Kick the ball harder to $\boxed{\text{increase } v_o \text{ and/or increase the angle}}$ so it is as close to 45° as possible.

76. At the maximum height, $y = R/2$ and $v_y = 0$. (Take $y_o = 0$.)

$$\text{Use the result from Exercise 3.71, } R = \frac{v_o^2 \sin 2\theta}{g}.$$

$$v_y^2 = v_{yo}^2 - 2gy, \quad \Rightarrow \quad 0 = v_o^2 \sin^2 \theta - 2gy_{\text{max}} = v_o^2 \sin^2 \theta - 2g \frac{v_o^2 \sin 2\theta}{g} = v_o^2 \sin^2 \theta - v_o^2 \sin 2\theta.$$

$$\text{So } v_o^2 \sin^2 \theta = v_o^2 \sin 2\theta \quad \text{or} \quad \sin^2 \theta = 2 \sin \theta \cos \theta.$$

$$\text{Therefore } \sin \theta = 2 \cos \theta \quad \text{or} \quad \tan \theta = 2. \quad \text{Thus } \theta = \boxed{63^\circ}.$$

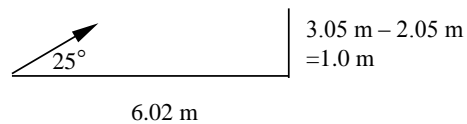
84. (Take both x_o and y_o as 0.)

$$x = x_o + v_{xo} t = (v_o \cos \theta)t, \quad \Rightarrow \quad t = \frac{x}{v_{xo}} = \frac{x}{v_o \cos \theta},$$

$$y = y_o + v_{yo} t - \frac{1}{2} g t^2 = v_o \sin \theta \times \frac{x}{v_o \cos \theta} - \frac{1}{2} g \left(\frac{x}{v_o \cos \theta} \right)^2 = x$$

$$\tan \theta - \frac{gx^2}{2v_o^2 \cos^2 \theta}.$$

$$\text{So } v_o = \frac{x}{\cos \theta} \sqrt{\frac{g}{2(x \tan \theta - y)}} = \frac{6.02 \text{ m}}{\cos 25^\circ} \sqrt{\frac{9.80 \text{ m/s}^2}{2[(6.02 \text{ m}) \tan 25^\circ - 1.0 \text{ m}]}]} = \boxed{10.9 \text{ m/s}}.$$



98. Use the following subscripts: b = boat, c = current, and w = water.

$$\text{Upstream: } v_{bc} = 7.5 \text{ m/s, } v_{cw} = -5.0 \text{ m/s.}$$

$$v_{bw} = v_{bc} + v_{cw} = 7.5 \text{ m/s} + (-5.0 \text{ m/s}) = 2.5 \text{ m/s.}$$

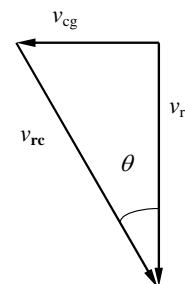
$$\text{So } t_{\text{up}} = \frac{500 \text{ m}}{2.5 \text{ m/s}} = 200 \text{ s.}$$

$$\text{Downstream: } v_{bc} = 7.5 \text{ m/s, } v_{cw} = 5.0 \text{ m/s. } v_{bw} = v_{bc} + v_{cw} = 7.5 \text{ m/s} + 5.0 \text{ m/s} = 12.5 \text{ m/s.}$$

$$\text{So } t_{\text{down}} = \frac{500 \text{ m}}{12.5 \text{ m/s}} = 40 \text{ s.}$$

Therefore $t = 200 \text{ s} + 40 \text{ s} = 240 \text{ s} = \boxed{4.0 \text{ min}}$.

102. (a) The relative velocity of the rain to that of the car is $\vec{v}_{rc} = \vec{v}_{rg} - \vec{v}_{cg}$, where the subscripts r, c, and g stand for rain, car, and ground, respectively, and the symbol \vec{v}_{cg} denotes the relative velocity of the car to the ground, etc. It is clear in the vector diagram that \vec{v}_{rc} is not vertical, but at an angle.



Since $\tan \theta = v_{cg}/v_{rg}$, the angle θ **also increases** as the velocity of the car increases.

(b) $v_{cg} = v_{rg} \tan \theta = (10 \text{ m/s}) \tan 25^\circ = \boxed{4.7 \text{ m/s}}$.

111. (a) $6000 \text{ km/h} = 167 \text{ m/s}$.

$$v_{x0} = v_o \cos 75^\circ = (166.7 \text{ m/s}) \cos 75^\circ = 43.1 \text{ m/s}, \quad v_{y0} = v_o \sin 75^\circ = (166.7 \text{ m/s}) \sin 75^\circ = 161 \text{ m/s}.$$

$$y = y_o + v_{y0} t - \frac{1}{2} g t^2, \quad \Rightarrow \quad 500 \text{ m} = 4000 \text{ m} + (161 \text{ m/s}) t - (4.90 \text{ m/s}^2) t^2.$$

Reducing to quadratic equation $4.9 t^2 - 161 t - 3500 = 0$.

Solving, $t = \boxed{47.8 \text{ s}}$ and -14.9 s .

(b) At the maximum height $v_y = 0$.

$$v_y^2 = v_{y0}^2 - 2g(y - y_o), \quad \Rightarrow \quad y = y_{\text{max}} = y_o + \frac{v_{y0}^2}{2g} = 4000 \text{ m} + \frac{(161 \text{ m/s})^2}{2(9.80 \text{ m/s}^2)} = \boxed{5.32 \times 10^3 \text{ m}}.$$

(c) $v_x = v_{x0} = 43.1 \text{ m/s}$,

$$v_y = v_{y0} - gt = 161 \text{ m/s} - (9.80 \text{ m/s}^2)(47.8 \text{ s}) = -307 \text{ m/s}.$$

$$\text{So } v_y = \sqrt{(43.1 \text{ m/s})^2 + (-307 \text{ m/s})^2} = \boxed{310 \text{ m/s}}.$$

112. $\vec{v}_A = (35 \text{ m/s}) \hat{x}$,

$$\vec{v}_B = [(30 \text{ m/s}) \cos 10^\circ] \hat{x} + [(30 \text{ m/s}) \sin 10^\circ] \hat{y} = (29.5 \text{ m/s}) \hat{x} + (5.21 \text{ m/s}) \hat{y}.$$

The velocity of car B relative to car A is

$$\vec{v}_B - \vec{v}_A = (29.5 \text{ m/s} - 35 \text{ m/s}) \hat{x} + (5.21 \text{ m/s}) \hat{y} = \boxed{(-5.5 \text{ m/s}) \hat{x} + (5.2 \text{ m/s}) \hat{y}}.$$

(b) Time for car A to get to point \otimes : $t_A = \frac{d_A}{v_A} = \frac{350 \text{ m}}{35 \text{ m/s}} = 10 \text{ s}$.

During that time car B will travel a distance of $d_B = v_B t = (30 \text{ m/s})(10 \text{ s}) = 300 \text{ m}$.

Since the angled ramp is longer than the straight ramp, car B will not be at point \otimes when car A is there.

Therefore they do *not* collide at point \otimes .

(c) The length of the 10° ramp is $d_B = \frac{350 \text{ m}}{\cos 10^\circ} = 355 \text{ m}$.

So the time for car B to reach point \otimes is $t_B = \frac{d_B}{v_B} = \frac{355 \text{ m}}{30 \text{ m/s}} = 11.8 \text{ s}$.

During the 11.8 s, car A will travel a total distance of $(35 \text{ m/s})(11.8 \text{ s}) = 413 \text{ m}$.

Therefore, when car B reaches point \otimes , car A will travel an extra distance of $413 \text{ m} - 350 \text{ m} = 63 \text{ m}$.

Thus, there is no collision.

Thus car A is $\boxed{63 \text{ m}}$ ahead.