

$$13. \quad F_{\text{net}} = ma, \quad \Rightarrow \quad m = \frac{F_{\text{net}}}{a} = \frac{4.0 \text{ N}}{10 \text{ m/s}^2} = \boxed{0.40 \text{ kg}}.$$

$$\boxed{14}. \quad \text{In the horizontal direction, } F_{\text{net}} = +30.0 \text{ N} + (-35.0 \text{ N}) = -5.0 \text{ N}.$$

$$F_{\text{net}} = ma, \quad \Rightarrow \quad a = \frac{F_{\text{net}}}{m} = \frac{-5.0 \text{ N}}{5.0 \text{ kg}} = \boxed{-1.0 \text{ m/s}^2}.$$

The negative sign indicates that the acceleration is in the  $-x$ -axis.

$$18. \quad \vec{F}_1 = (5.5 \text{ N})[(\cos 30^\circ) \hat{x} - (\sin 30^\circ) \hat{y}] = (4.76 \text{ N}) \hat{x} + (-2.75 \text{ N}) \hat{y},$$

$$\vec{F}_2 = (3.5 \text{ N})[(\cos 37^\circ) \hat{x} + (\sin 37^\circ) \hat{y}] = (2.80 \text{ N}) \hat{x} + (2.11 \text{ N}) \hat{y}.$$

$$\Sigma \vec{F} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 = 0, \quad \Rightarrow \quad \vec{F}_3 = -(\vec{F}_1 + \vec{F}_2) = \boxed{(-7.6 \text{ N}) \hat{x} + (0.64 \text{ N}) \hat{y}}.$$

22. (a) For the net force to be zero, the unknown (3<sup>rd</sup> force) must be in

$\boxed{(2) \text{ the second quadrant}}$ . The  $x$ -component of the unknown force must be

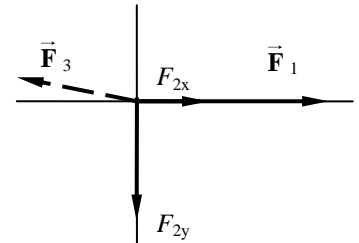
due west and the  $y$ -component of the unknown force must be due north.

$$(b) \text{ From } \Sigma \vec{F} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 = 0,$$

$$\vec{F}_3 = 0 - (\vec{F}_1 + \vec{F}_2) = -\vec{F}_1 - \vec{F}_2$$

$$= [-(150 \text{ lb}) - (30.0 \text{ lb})] \hat{x} - (-40.0 \text{ lb}) \hat{y} = (-180 \text{ N}) \hat{x} + (40.0 \text{ N}) \hat{y},$$

$$\text{or } F_3 = \sqrt{(-180 \text{ N})^2 + (40.0 \text{ N})^2} = \boxed{184 \text{ N}}, \quad \theta = \tan^{-1}\left(\frac{40.0 \text{ N}}{-180 \text{ N}}\right) = \boxed{12.5^\circ \text{ above the } -x\text{-axis}}.$$



$$39. \quad \text{The friction force is opposite the horizontal force. } a = \frac{F_{\text{net}}}{m} = \frac{300 \text{ N} - 120 \text{ N}}{75 \text{ kg}} = \boxed{2.40 \text{ m/s}^2}.$$

45. First find the acceleration from dynamics. The acceleration is in the horizontal direction.

$$\Sigma F_x = -(1.30 \times 10^4 \text{ N}) \cos 30^\circ = -1.126 \times 10^4 \text{ N}.$$

$$\Sigma F_x = ma, \quad \Rightarrow \quad a = \frac{\Sigma F_x}{m} = \frac{-1.126 \times 10^4 \text{ N}}{2000 \text{ kg}} = -5.629 \text{ m/s}^2.$$

$$v_o = 45.0 \text{ m/s}, \quad v = 0 \text{ (stop)}, \quad a = -5.629 \text{ m/s}^2.$$

$$v^2 = v_o^2 + 2a(x - x_o), \quad \Rightarrow \quad x - x_o = \frac{v^2 - v_o^2}{2a} = \frac{0^2 - (45.0 \text{ m/s})^2}{2(-5.629 \text{ m/s}^2)} = 180 \text{ m} < 200 \text{ m}.$$

$\boxed{\text{Lois is saved}}$ .

54. (a) For Jane:  $T = ma = (50 \text{ kg})(0.92 \text{ m/s}^2) = 46 \text{ N}$ .

The force on John is also 46 N (Newton's 3<sup>rd</sup> law).

$$a_{\text{John}} = \frac{46 \text{ N}}{60 \text{ kg}} = \boxed{0.77 \text{ m/s}^2 \text{ toward Jane}}.$$

(b)  $x_{\text{John}} = \frac{1}{2} a_{\text{John}} t^2$ ,  $x_{\text{Jane}} = \frac{1}{2} a_{\text{Jane}} t^2$ .

So  $\frac{x_{\text{Jane}}}{x_{\text{John}}} = \frac{a_{\text{Jane}}}{a_{\text{John}}} = \frac{0.92}{0.767} = 1.2$ .

Also  $x_{\text{John}} + x_{\text{Jane}} = 10 \text{ m}$ , or  $x_{\text{John}} + 1.2 x_{\text{John}} = 10 \text{ m}$ .

Therefore  $x_{\text{John}} = \boxed{4.5 \text{ m from John's original position}}$ .

55. (a) The answer is  $\boxed{(4) \text{ the pull of the rope on the girl}}$ . The pull of the rope on the girl is the reaction of the pull of the girl on the rope.

(b)  $\Sigma F_y = T - w = T - mg = ma$ ,

so  $T = m(a + g) = (25.0 \text{ kg})(0.75 \text{ m/s}^2 + 9.80 \text{ m/s}^2) = \boxed{264 \text{ N}}$ .

65. (a)  $\vec{F}_1 = (400 \text{ N}) \hat{x}$ ,  $\vec{F}_2 = (-300 \text{ N}) \hat{x}$ ,

$$\vec{F}_3 = (50 \text{ N})[(\cos 60^\circ) \hat{x} + (\sin 60^\circ) \hat{y}] = (25.0 \text{ N}) \hat{x} + (43.3 \text{ N}) \hat{y}.$$

$$\Sigma \vec{F} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 = (125 \text{ N}) \hat{x} + (43.3 \text{ N}) \hat{y}.$$

So  $\vec{a} = \frac{\Sigma \vec{F}}{m} = \frac{(125 \text{ N}) \hat{x} + (43.3 \text{ N}) \hat{y}}{75 \text{ kg}} = (1.67 \text{ m/s}^2) \hat{x} + (0.577 \text{ m/s}^2) \hat{y}$ .

$$a = \sqrt{(1.67 \text{ m/s}^2)^2 + (0.577 \text{ m/s}^2)^2} = \boxed{1.7 \text{ m/s}^2},$$

$$\theta = \tan^{-1} \left( \frac{0.577}{1.67} \right) = \boxed{19^\circ \text{ north of east}}.$$

(b) Now the wind and current force is opposite that of Part (a).

$$\vec{F}_3 = -[(25.0 \text{ N}) \hat{x} + (43.3 \text{ N}) \hat{y}]. \quad \Sigma \vec{F} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 = (75 \text{ N}) \hat{x} + (-43.3 \text{ N}) \hat{y}.$$

$$\vec{a} = (1.00 \text{ m/s}^2) \hat{x} + (-0.577 \text{ m/s}^2) \hat{y}.$$

$$a = \sqrt{(1.00 \text{ m/s}^2)^2 + (-0.577 \text{ m/s}^2)^2} = \boxed{1.2 \text{ m/s}^2}.$$

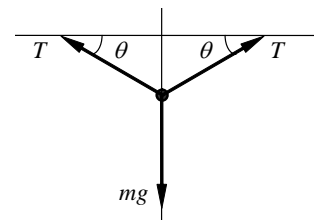
$$\theta = \tan^{-1} \left( \frac{-0.577}{1.00} \right) = \boxed{30^\circ \text{ south of east}}.$$

73. (a) The angle the rope makes with the horizontal,  $\theta$ , depends on both the tree

separation and sag.  $\Sigma F_y = 2T \sin \theta - mg = 0$ ,  $T = \frac{mg}{2 \sin \theta}$ .

So the tension depends on  $\boxed{(3) \text{ both the tree separation and sag}}$ .

(b)  $\theta = \tan^{-1} \left( \frac{0.20 \text{ m}}{5.0 \text{ m}} \right) = 2.29^\circ$ .  $T = \frac{(5.0 \text{ kg})(9.80 \text{ m/s}^2)}{2 \sin 2.29^\circ} = \boxed{6.1 \times 10^2 \text{ N}}$ .



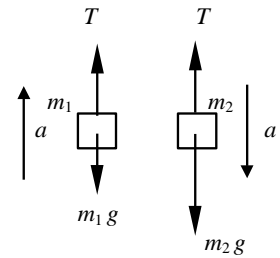
80. (a) Since the two objects accelerate together, they have the same acceleration,  $a$ . Also according to Newton's third law, the tension on  $m_1$  (up) is the same as the tension on  $m_2$  (up).

$$\text{For } m_1: \quad \Sigma F_1 = T - m_1 g = m_1 a. \quad (1)$$

$$\text{For } m_2: \quad \Sigma F_2 = m_2 g - T = m_2 a. \quad (2)$$

$$\text{Equation (1) + Equation (2) gives } (m_2 - m_1)g = (m_1 + m_2)a,$$

$$\text{so } a = \frac{(m_2 - m_1)g}{m_1 + m_2} = \frac{(0.80 \text{ kg} - 0.55 \text{ kg})(9.80 \text{ m/s}^2)}{0.55 \text{ kg} + 0.80 \text{ kg}} = \boxed{1.8 \text{ m/s}^2}.$$



$$\text{(b) From Equation (1), } T = m_1(a + g) = (0.55 \text{ kg})(1.8 \text{ m/s}^2 + 9.80 \text{ m/s}^2) = \boxed{6.4 \text{ N}}.$$

83. (a) According to Newton's 3<sup>rd</sup> law, the tension force at the ends of the string are the same because the string is massless. Since  $m_2$  is accelerating up,  $T > w_2$ . Since  $F$  is responsible for accelerating both  $m_1$  and  $m_2$  upward,  $F > T$ . Therefore the answer is

$$\boxed{(1) T > w_2 \text{ and } T < F}.$$

$$\text{(b) For } m_1: \quad \Sigma F_1 = F - T - m_1 g = m_1 a \quad (1)$$

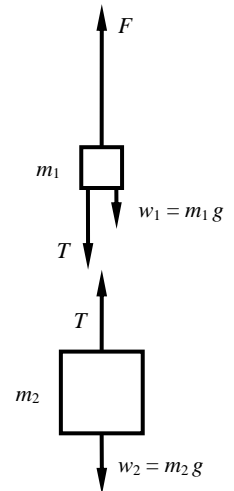
$$\text{For } m_2: \quad \Sigma F_2 = T - m_2 g = m_2 a \quad (2)$$

$$\text{Equation (1) + Equation (2) gives}$$

$$F - m_1 g - m_2 g = m_1 a + m_2 a = (m_1 + m_2)a.$$

$$F = (m_1 + m_2)(a + g) = (50.0 \text{ kg} + 100 \text{ kg})(1.50 \text{ m/s}^2 + 9.80 \text{ m/s}^2) = \boxed{1.70 \times 10^3 \text{ N}}.$$

$$\text{(c) From Equation (2), } T = m_2(a + g) = (100 \text{ kg})(1.50 \text{ m/s}^2 + 9.80 \text{ m/s}^2) = \boxed{1.13 \times 10^3 \text{ N}}.$$



100. (a) First find acceleration from dynamics and use  $\mu_k$  from Table 4.1.

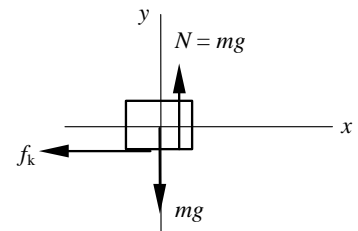
$$\Sigma F_x = -f_k = -\mu_k mg = ma, \quad \Rightarrow \quad \mu_k = -\frac{a}{g}.$$

$$\text{So } a = -\mu_k g = -0.85(9.80 \text{ m/s}^2) = -8.33 \text{ m/s}^2,$$

$$\text{and } v_o = 90 \text{ km/h} = 25 \text{ m/s}, \quad v = 0. \quad (\text{Take } x_o = 0.)$$

$$v^2 = v_o^2 + 2a(x - x_o), \quad \Rightarrow \quad x = \frac{v^2 - v_o^2}{2a} = \frac{0 - (25 \text{ m/s})^2}{2(-8.33 \text{ m/s}^2)} = \boxed{38 \text{ m}}.$$

$$\text{(b) } a = -0.60(9.80 \text{ m/s}^2) = -5.88 \text{ m/s}^2. \quad \text{So } x = \frac{0 - (25 \text{ m/s})^2}{2(-5.88 \text{ m/s}^2)} = \boxed{53 \text{ m}}.$$



101. Use the result of 4.100(a),  $\mu_k = -\frac{a}{g}$ .

$$a = \frac{0 - (5.0 \text{ m/s})^2}{2(20 \text{ m})} = -0.625 \text{ m/s}^2, \quad \text{so } \mu_k = -\frac{-0.625 \text{ m/s}^2}{9.80 \text{ m/s}^2} = \boxed{0.064}.$$

111. Use the diagram in Exercise 4.110 but with  $f_k$  replacing  $f_s$ .

$$\text{For } m_1: \Sigma F_1 = T_1 - m_1 g = m_1 a, \quad (1)$$

$$\text{For } m_3: \Sigma F_3 = T_2 - T_1 - f_k = m_3 a, \quad (2), \text{ where } f_k = \mu_k N_3 = \mu_k m_3 g.$$

$$\text{For } m_2: \Sigma F_2 = m_2 g - T_2 = m_2 a, \quad (3)$$

$$\text{Equation (1) + Equation (2) + Equation (3) gives } (m_2 - m_1 - \mu_k m_3)g = (m_1 + m_2 + m_3)a,$$

$$\text{so } a = \frac{(m_2 - m_1 - \mu_k m_3)g}{m_1 + m_2 + m_3}.$$

$$(a) \text{ For constant speed, } a = 0. \text{ So } m_3 = \frac{m_2 - m_1}{\mu_k} = \frac{0.250 \text{ kg} - 0.150 \text{ kg}}{0.560} = \boxed{0.179 \text{ kg}}.$$

$$(b) a = \frac{0.250 \text{ kg} - 0.150 \text{ kg} - (0.560)(0.100 \text{ kg})}{0.150 \text{ kg} + 0.250 \text{ kg} + 0.100 \text{ kg}} (9.80 \text{ m/s}^2) = \boxed{0.862 \text{ m/s}^2}.$$

**117.** (a) If  $m$  is accelerating upward,  $M$  is accelerating down the incline.

$$\text{For } M: \Sigma F_y = N - Mg \cos \theta = 0,$$

$$\text{so } N = Mg \cos \theta = (5.00 \text{ kg})(9.80 \text{ m/s}^2) \cos 30^\circ = 42.4 \text{ N}.$$

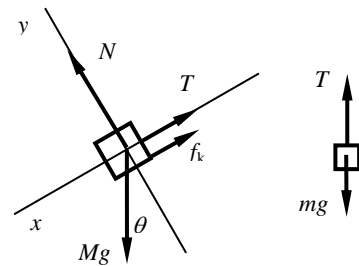
$$f_k = \mu_k N = (0.100)(42.4 \text{ N}) = 4.24 \text{ N}.$$

$$\Sigma F_x = Mg \sin \theta - T - f_k = Ma, \quad \text{so}$$

$$T = Mg \sin \theta - f_k - Ma$$

$$= (5.00 \text{ kg})(9.80 \text{ m/s}^2) \sin 30^\circ - 4.24 \text{ N} - (5.00 \text{ kg})(2.00 \text{ m/s}^2)$$

$$= \boxed{10.3 \text{ N}}.$$



$$(b) \text{ For } m: \Sigma F_x = T - mg = ma, \quad \Rightarrow \quad m = \frac{T}{g + a} = \frac{10.3 \text{ N}}{9.80 \text{ m/s}^2 + 2.00 \text{ m/s}^2} = \boxed{0.954 \text{ kg}}.$$