

$$\boxed{8.} \quad W = F \cos \theta d, \quad \Rightarrow \quad F = \frac{W}{d \cos \theta} = \frac{50 \text{ J}}{(10 \text{ m}) \cos 0^\circ} = \boxed{5.0 \text{ N}}.$$

9. The friction force is  $f_k = \mu_k N = \mu_k mg$ , and the angle between the friction force and displacement is  $180^\circ$ .

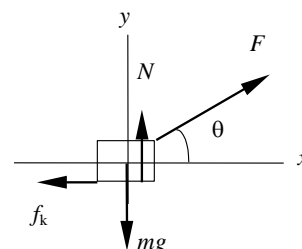
$$\text{So } W = F \cos \theta d = \mu_k mg \cos \theta d = 0.20(5.0 \text{ kg})(9.80 \text{ m/s}^2) \cos 180^\circ (10 \text{ m}) = \boxed{-98 \text{ J}}.$$

$$\boxed{14.} \quad \Sigma F_y = N + F \sin \theta - mg = 0, \quad N = mg - F \sin \theta.$$

$$\Sigma F_x = F \cos \theta - f_k = 0, \quad \text{or } F \cos \theta = \mu_k N = \mu_k (mg - F \sin \theta) = 0.$$

$$\text{So } F = \frac{\mu_k mg}{\cos \theta + \mu_k \sin \theta} = \frac{0.20(35 \text{ kg})(9.80 \text{ m/s}^2)}{\cos 30^\circ + 0.20 \sin 30^\circ} = 71.0 \text{ N}.$$

$$\text{Therefore } W = F \cos \theta d = (71.0 \text{ N}) \cos 30^\circ (10 \text{ m}) = \boxed{6.1 \times 10^2 \text{ J}}$$



$$20. \quad f_k = \mu_k N = \mu_k mg = (0.600)(100 \text{ kg})(9.80 \text{ m/s}^2) = 588 \text{ N}.$$

$$f_s = \mu_s N = \mu_s mg = (0.750)(100 \text{ kg})(9.80 \text{ m/s}^2) = 735 \text{ N}.$$

A force equal to  $f_s = 735 \text{ N}$  is required to move the desk.

Once the desk starts moving, the applied force creates acceleration, because the friction force is kinetic now.

$$\Sigma F = 735 \text{ N} - 588 \text{ N} = 147 \text{ N} = ma, \quad \Rightarrow \quad a = \frac{147 \text{ N}}{100 \text{ kg}} = 1.47 \text{ m/s}^2.$$

$$d = (x - x_0) = v_0 t + \frac{1}{2} a t^2 = 0 + \frac{1}{2} (1.47 \text{ m/s}^2)(5.00 \text{ s})^2 = 18.375 \text{ m}.$$

$$W = F \cos \theta d = (735 \text{ N}) \cos 0^\circ (18.375 \text{ m}) = \boxed{1.35 \times 10^4 \text{ J}}.$$

23. **No**, it takes more work. This is because the **force increases as the spring stretches**, according to Hooke's law:  $F_s = -kx$ . Also the displacement is greater.

$$24. \quad (\text{d}) \quad W = \frac{1}{2} k (x^2 - x_0^2), \quad \Rightarrow \quad \frac{W_2}{W_1} = \frac{x_2^2 - x_1^2}{x_1^2 - x_0^2} = \frac{4.0^2 - 2.0^2}{2.0^2 - 0^2} = 3 \quad \text{so } \boxed{\text{three times as much}}.$$

$$25. \quad F_s = -kx, \quad \Rightarrow \quad k = \left| \frac{F_s}{x} \right| = \frac{4.0 \text{ N}}{0.050 \text{ m}} = \boxed{80 \text{ N/m}}.$$

$$\boxed{26.} \quad W = \frac{1}{2} kx^2 = \frac{1}{2} (30 \text{ N/m})(0.020 \text{ m})^2 = \boxed{6.0 \times 10^{-3} \text{ J}}.$$

$$27. \quad W = \frac{1}{2} kx^2, \quad \Rightarrow \quad k = \frac{2W}{x^2} = \frac{2(400 \text{ J})}{(0.0800 \text{ m})^2} = \boxed{1.25 \times 10^5 \text{ N/m}}.$$

$$33. \quad (\text{a}) \quad W = \frac{1}{2} kx^2 = \frac{1}{2} (2.5 \times 10^3 \text{ N/m})(0.060 \text{ m})^2 = \boxed{4.5 \text{ J}}.$$

$$(\text{b}) \quad \text{The difference in work is } \Delta W = \frac{1}{2} k(x_2^2 - x_1^2) = \frac{1}{2} (2.5 \times 10^3 \text{ N/m})[(0.080 \text{ m})^2 - (0.060 \text{ m})^2] = \boxed{3.5 \text{ J}}.$$

35. Work is equal to the area under the force versus displacement curve. There are two areas. The first one is a triangle starting from the origin.  

$$W_1 = \frac{1}{2} (20 \text{ N})(0.30 \text{ m}) = 3.0 \text{ J}.$$
 The second one is a triangle plus a rectangle.  

$$W_2 = \frac{1}{2} (20 \text{ N})(0.10 \text{ m}) + (20 \text{ N})(0.10 \text{ m}) = 3.0 \text{ J}.$$
 Therefore the total work is  $3.0 \text{ J} + 3.0 \text{ J} = \boxed{6.0 \text{ J}}$ .
38. (b), because  $\cos \theta < 0$  for  $90^\circ < \theta < 270^\circ$  and  $W = F \cos \theta d = \Delta K$ . So  $K$  decreases.
39. (c). The kinetic energy of each car is the same, and let's assume it is  $K$ . For the two cars colliding head on, the total kinetic energy is  $2K$ , and that amount is shared by the two cars, so each gets  $K$  and that energy causes certain amount of damage. For the car that crashed into a wall, the total kinetic energy is  $K$ , but that is shared by the car and the wall. So the car into the wall absorbs less energy and therefore less damage.
40. (a).  $K = \frac{1}{2} m v^2$ .  

$$K_a = \frac{1}{2} (4m)v^2 = 2mv^2; \quad K_b = \frac{1}{2} (3m)(2v)^2 = 6mv^2;$$

$$K_c = \frac{1}{2} (3m)(3v)^2 = 13.5mv^2; \quad K_d = \frac{1}{2} (2m)(3v)^2 = 9mv^2.$$
41. Reducing speed by half. Since  $K = \frac{1}{2} m v^2$ , reducing the speed by half will reduce  $K$  by  $\frac{3}{4}$ , whereas reducing the mass by half will only reduce  $K$  by half.
46. (a)  $90 \text{ km/h} = 25 \text{ m/s}$ .  $K_o = \frac{1}{2} m v_o^2 = \frac{1}{2} (1.2 \times 10^3 \text{ kg})(25 \text{ m/s})^2 = \boxed{3.8 \times 10^5 \text{ J}}$ .  
 (b)  $W = \frac{1}{2} m v^2 - \frac{1}{2} m v_o^2 = 0 - 3.8 \times 10^5 \text{ J} = \boxed{-3.8 \times 10^5 \text{ J}}$ .
51. For an object on an incline, the normal force is equal to  $n = mg \cos \theta$ . (See Exercise 4.61b.)  

$$f_k = \mu_k N = \mu_k mg \cos \theta = (0.30)(5000 \text{ kg})(9.80 \text{ m/s}^2) \cos 15^\circ = 1.42 \times 10^4 \text{ N}.$$
 Two forces are doing non-zero work, the frictional force and the gravitational force.  

$$W = \frac{1}{2} m v^2 - \frac{1}{2} m v_o^2, \quad \Rightarrow \quad f_k \cos 180^\circ x + mg \cos (90 - \theta) x = \frac{1}{2} m v^2 - \frac{1}{2} m v_o^2 = 0 - \frac{1}{2} m v_o^2.$$

$$-(1.42 \times 10^4 \text{ N})x + (5000 \text{ kg})(9.80 \text{ m/s}^2)(\sin 15^\circ)x = -\frac{1}{2} (5000 \text{ kg})(35.0 \text{ m/s})^2,$$
 solving,  $x = \boxed{2.0 \times 10^3 \text{ m}}$ .
56.  $U = \frac{1}{2} k x^2$ , so  $\Delta U = \frac{1}{2} k(x^2 - x_o^2) \propto \boxed{x^2 - x_o^2}$ .
57. They will have the same potential energy at the top because they have the same height. ( $U = mgy$ )
58.  $U = mgy$ ,  $\Rightarrow \Delta U = mg\Delta y = (1.0 \text{ kg})(9.80 \text{ m/s}^2)(1.2 \text{ m} - 0.90 \text{ m}) = \boxed{2.9 \text{ J}}$ .

65. (a) The component of the weight,  $mg$ , of the object along the incline (parallel to the spring) is equal to  $mg \sin \theta$ . (See Exercise 4-69.) This is the force that stretches the spring.

$$x = \left| \frac{F_s}{k} \right| = \frac{mg \sin \theta}{k} = \frac{(1.50 \text{ kg})(9.80 \text{ m/s}^2) \sin 30^\circ}{175 \text{ N/m}} = 0.0420 \text{ m}.$$

$$\Delta U_s = \frac{1}{2} k x^2 - \frac{1}{2} k x_o^2 = \frac{1}{2} (175 \text{ N/m})(0.0420 \text{ m})^2 - 0 = \boxed{0.154 \text{ J}}.$$

- (b) The vertical distance the mass moves down is equal to  $x \sin \theta = (0.0420 \text{ m}) \sin 30^\circ = 0.0210 \text{ m}$ .

$$\Delta U_g = mg\Delta y = (1.50 \text{ kg})(9.80 \text{ m/s}^2)(-0.0210 \text{ m} - 0) = \boxed{-0.309 \text{ J}}.$$

76. The total mechanical energy is conserved, because there are no non-conservative forces that are doing work.

When  $m$  falls 1.00 m,  $M$  will move up the incline 1.00 m and therefore move up (vertically) a distance of

$$(1.00 \text{ m}) \sin 5^\circ = 0.0872 \text{ m}. \quad \frac{1}{2} M v^2 + \frac{1}{2} m v^2 + \Delta U_M + \Delta U_m = 0. \quad \text{So,}$$

$$\frac{1}{2} (1.00 \text{ kg} + 0.200 \text{ kg}) v^2 + (1.00 \text{ kg})(9.80 \text{ m/s}^2)(0.0872 \text{ m}) - (0.200 \text{ kg})(9.80 \text{ m/s}^2)(1.00 \text{ m}) = 0.$$

79. (a)  $\frac{y_1}{y_o} = \frac{E_1}{E_o} = 0.820$ ,  $y_1 = 0.820 y_o = (0.820)(1.25 \text{ m}) = \boxed{1.03 \text{ m}}$ .

(b)  $y_2 = 0.82y_1 = (0.820)(1.025 \text{ m}) = \boxed{0.841 \text{ m}}$ .

- (c) The kinetic energy of the ball must be equal to the lost mechanical energy.

$$K_o = 0.180 E_o = 0.180 (K_o + U_o), \quad \text{so} \quad K_o = \frac{0.180 U_o}{0.820} = 0.2195 U_o = 0.2195 mg (1.25 \text{ m}) = \frac{1}{2} m v_o^2.$$

$$\text{Therefore} \quad v_o = \sqrt{2(0.2195)(9.80 \text{ m/s}^2)(1.25 \text{ m})} = \boxed{2.32 \text{ m/s}}.$$

$$\text{Solving,} \quad v = \boxed{1.36 \text{ m/s}}.$$

88. When  $m$  moves with 1.50 m/s,  $M$  also moves with the same speed. Mechanical energy is conserved here. If  $m$  moves down a distance  $y$ ,  $M$  will move up (vertically) a distance of  $y \sin 20^\circ$ , and the spring will stretch a distance of  $y$ .

$$K_{oM} + K_{om} + U_{oM} + U_{om} + U_{os} = K_M + K_m + U_M + U_m + U_s.$$

$$K_M = K_m = 0 \text{ (coming to rest)}. \quad \frac{1}{2} (M + m) v_o^2 = mg(-y) + Mgy(\sin 20^\circ) + \frac{1}{2} k y^2.$$

$$\text{Reducing to quadratic equation:} \quad 12.5 y^2 + 2.96y - 1.17 = 0.$$

$$\text{Solving,} \quad y = \boxed{0.21 \text{ m}}.$$

91.  $\boxed{\text{No, paying for energy}}$  because kWh is the unit of power  $\times$  time = energy.

$$2.5 \text{ kWh} = 2500 \text{ Wh} = (2500 \text{ Wh}) \times \frac{3600 \text{ s}}{1 \text{ h}} = \boxed{9.0 \times 10^6 \text{ J}}.$$

101. (a)  $P = \frac{W}{t} = \frac{Fd}{t} = \frac{mgd}{t} = \frac{(70 \text{ kg})(9.80 \text{ m/s}^2)(8.0 \text{ m})}{10 \text{ s}} = \boxed{5.5 \times 10^2 \text{ W}}$ .

$$(b) (5.5 \times 10^2 \text{ W}) \times \frac{1 \text{ hp}}{746 \text{ W}} = \boxed{0.74 \text{ hp}}.$$

103. 850 km/h = 236.1 m/s. The work required is

$$W = \Delta E = K + U = \frac{1}{2}(3.25 \times 10^3 \text{ kg})(236.1 \text{ m/s})^2 + (3.25 \times 10^3 \text{ kg})(9.80 \text{ m/s}^2)(10.0 \times 10^3 \text{ m}) \\ = 4.091 \times 10^8 \text{ J}.$$

The energy output is  $E = Pt = (1500 \text{ hp})(746 \text{ W/hp})(12.5 \text{ min})(60 \text{ s/min}) = 8.393 \times 10^8 \text{ J}$ .

$$\text{So the efficiency is } \varepsilon = \frac{4.091}{8.393} = \boxed{48.7\%}.$$

109. Choose the bottom of the swing as the reference level for gravitational potential energy. The total initial mechanical energy is all gravitational potential.

$$E_o = mgy_o.$$

From Exercise 5-82, the initial height relative to the bottom of the swing is  $y_o = L(1 - \cos\theta)$ .

When he stops, the mechanical energy is zero, and this is due to the work done by the kinetic frictional force (non-conservative force). The friction force is equal to  $f_k = \mu_k N = \mu_k mg$ .

$$W_{nc} = E - E_o, \quad \Rightarrow \quad f_k \cos 180^\circ d = -\mu_k mgd = 0 - mgL(1 - \cos\theta).$$

$$\text{So } d = \frac{L(1 - \cos\theta)}{\mu_k} = \frac{(15.0 \text{ m})(1 - \cos 60^\circ)}{0.75} = \boxed{10 \text{ m}}.$$