

$$\boxed{8}. \quad \begin{array}{ll} \text{(a)} (15^\circ) \times \frac{\pi \text{ rad}}{180^\circ} = \boxed{0.26 \text{ rad}}. & \text{(b)} (45^\circ) \times \frac{\pi \text{ rad}}{180^\circ} = \boxed{0.79 \text{ rad}}. \\ \text{(c)} (90^\circ) \times \frac{\pi \text{ rad}}{180^\circ} = \boxed{1.6 \text{ rad}}. & \text{(d)} (120^\circ) \times \frac{\pi \text{ rad}}{180^\circ} = \boxed{2.1 \text{ rad}}. \end{array}$$

$$9. \quad \begin{array}{ll} \text{(a)} (\pi/6 \text{ rad}) \times \frac{180^\circ}{\pi \text{ rad}} = \boxed{30^\circ}. & \text{(b)} (5\pi/12 \text{ rad}) \times \frac{180^\circ}{\pi \text{ rad}} = \boxed{75^\circ}. \\ \text{(c)} (3\pi/4 \text{ rad}) \times \frac{180^\circ}{\pi \text{ rad}} = \boxed{135^\circ}. & \text{(d)} (\pi \text{ rad}) \times \frac{180^\circ}{\pi \text{ rad}} = \boxed{180^\circ}. \end{array}$$

$$17. \quad s = r\theta = (0.600 \text{ m})(7.50 \text{ rev}) \times \frac{2\pi \text{ rad}}{1 \text{ rev}} = \boxed{28.3 \text{ m}}.$$

$$\boxed{28}. \quad \omega = \frac{\Delta\theta}{\Delta t} = \frac{2.5(2\pi \text{ rad})}{(3.0 \text{ min})(60 \text{ s/min})} = \boxed{0.087 \text{ rad/s}}.$$

$$29. \quad \omega = \frac{\Delta\theta}{\Delta t}, \quad \Delta t = \frac{\Delta\theta}{\omega} = \frac{2\pi \text{ rad}}{3.5 \text{ rad/s}} = \boxed{1.8 \text{ s}}$$

$$36. \quad \bar{v} = \frac{\Delta x}{\Delta t} = \frac{2.55 \text{ m}}{2.30 \text{ s}} = 1.11 \text{ m/s}. \quad \bar{v} = r\bar{\omega}, \quad \bar{\omega} = \frac{\bar{v}}{r} = \frac{1.109 \text{ m/s}}{1.75 \text{ m}} = \boxed{0.634 \text{ rad/s}}.$$

As calculated, the tangential speed is $\boxed{1.11 \text{ m/s}}$.

$$37. \quad \text{(a)} v = r\omega, \quad \omega = \frac{v}{r} = \frac{15 \text{ m/s}}{(120 \text{ m})/2} = 0.25 \text{ rad/s}.$$

$$\theta = \omega\Delta t = (0.25 \text{ rad/s})(4.00 \text{ min})(60 \text{ s/min}) = \boxed{60 \text{ rad}}.$$

$$\text{(b)} s = r\theta = \frac{120 \text{ m}}{2} \times (60 \text{ rad}) = \boxed{3.6 \times 10^3 \text{ m}}.$$

$$48. \quad a_c = r\omega^2, \quad \omega = \sqrt{\frac{a_c}{r}} = \sqrt{\frac{9.80 \text{ m/s}^2}{(35000 \text{ m})}} = \boxed{0.053 \text{ rad/s or about 730 rev/day}}.$$

$$49. \quad a_c = r\omega^2 = (3.80 \times 10^8 \text{ m}) \left[\frac{2\pi \text{ rad}}{(27.3 \text{ day})(86400 \text{ s/day})} \right]^2 = \boxed{2.69 \times 10^{-3} \text{ m/s}^2}.$$

55. The radius is $\frac{56.0 \text{ cm}}{2} = 28.0 \text{ cm} = 0.280 \text{ m}$. In one period, each mass travels a tangential distance that is equal to the circumference of a circle of radius 0.280 m. The tangential speed is then $v = \frac{2\pi(0.280 \text{ m})}{0.750 \text{ s}} = 2.345 \text{ m/s}$.

$$F_c = m \frac{v^2}{r} = (1.50 \text{ kg}) \times \frac{(2.345 \text{ m/s})^2}{0.280 \text{ m}} = \boxed{29.5 \text{ N}} < 100 \text{ N}. \quad \text{The } \boxed{\text{string will work}}.$$

$\boxed{56}$. (a) The normal force is greater $\boxed{\text{at the bottom}}$, because at that position, the normal force has to provide the upward centripetal force, in addition to supporting the weight of the pilot.

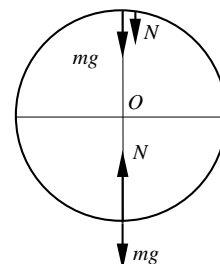
(b) $700 \text{ km/h} = 194 \text{ m/s}$. At the bottom, the centripetal force is provided by the difference

$$N - mg. \quad \text{So } F_c = N - mg = m \frac{v^2}{r},$$

$$N = mg + m \frac{v^2}{r} = mg + m \frac{(194 \text{ m/s})^2}{2.0 \times 10^3 \text{ m}} = mg + m(18.8 \text{ m/s}^2) = mg + 1.9mg = \boxed{2.9mg}.$$

(b) At the top, the centripetal force is provided by $N + mg$.

$$N = m \frac{v^2}{r} - mg = m \frac{(194 \text{ m/s})^2}{2.0 \times 10^3 \text{ m}} - mg = m(18.8 \text{ m/s}^2) - mg = 1.93mg - mg = \boxed{0.93mg}.$$



66. $700 \text{ rpm} = 73.3 \text{ rad/s}$, $3000 \text{ rpm} = 314 \text{ rad/s}$. $\alpha = \frac{\Delta\omega}{\Delta t} = \frac{314 \text{ rad/s} - 73.3 \text{ rad/s}}{3.0 \text{ s}} = \boxed{80 \text{ rad/s}^2}$.

67. Given: $\omega_0 = 0$, $\omega = 2.5 \text{ rpm} = 0.262 \text{ rad/s}$, $\theta = 5.0 \text{ rev} = 10\pi \text{ rad}$. Find: α .

$$\omega^2 = \omega_0^2 + 2\alpha\theta, \quad \alpha = \frac{\omega^2 - \omega_0^2}{2\theta} = \frac{(0.262 \text{ rad/s})^2 - 0}{2(10\pi \text{ rad})} = \boxed{1.1 \times 10^{-3} \text{ rad/s}^2}$$

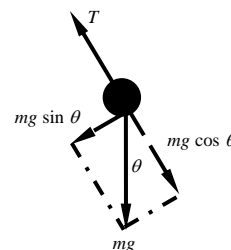
72. (a) In the tangential direction, $\Sigma F = mg \sin \theta = ma_t$.

So $a_t = g \sin \theta = (9.80 \text{ m/s}^2) \sin 15^\circ = \boxed{2.5 \text{ m/s}^2}$.

$$a_c = \frac{v^2}{r} = \frac{(2.7 \text{ m/s})^2}{0.75 \text{ m}} = \boxed{9.7 \text{ m/s}^2}$$

(b) At the **lowest point** of the swing, since v is maximum there.

$a_t = \boxed{0}$ since $\theta = 0$ so $\sin \theta = 0$.



76. (d), because $a_g = \frac{GM_E}{(R_E + h)^2}$. When $h = R_E$, a_g becomes $\frac{1}{2^2} = \frac{1}{4}$ as large.

80. $g_M = \frac{GM_M}{R_M^2} = \frac{(6.67 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2)(7.4 \times 10^{22} \text{ kg})}{(1.75 \times 10^6 \text{ m})^2} = \boxed{1.6 \text{ m/s}^2}$.

81. $F = \frac{GM_E M_M}{r_{E-M}^2} = \frac{(6.67 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2)(5.98 \times 10^{24} \text{ kg})(7.4 \times 10^{22} \text{ kg})}{(3.8 \times 10^8 \text{ m})^2} = \boxed{2.0 \times 10^{20} \text{ N}}$.

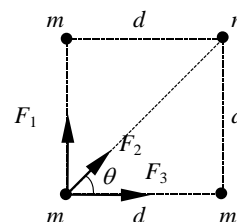
83. $F_1 = F_3 = \frac{Gm^2}{d^2} = \frac{(6.67 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2)(2.5 \text{ kg})^2}{(1.0 \text{ m})^2} = 4.17 \times 10^{-10} \text{ N}$,

The diagonal distance is $\sqrt{(1.0 \text{ m})^2 + (1.0 \text{ m})^2} = \sqrt{2} \text{ m}$,

so $F_2 = \frac{(6.67 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2)(2.5 \text{ kg})^2}{(\sqrt{2} \text{ m})^2} = 2.08 \times 10^{-10} \text{ N}$.

From symmetry the net force is

$$F = \sqrt{(4.17 \times 10^{-10} \text{ N})^2 + (4.17 \times 10^{-10} \text{ N})^2} + 2.08 \times 10^{-10} \text{ N} \\ = \boxed{8.0 \times 10^{-10} \text{ N, toward opposite corner}}$$



98. The Kepler constant for orbiting Mars is

$$K_M = \frac{4\pi^2}{Gm_M} = \frac{4\pi^2}{(6.67 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2)(6.4 \times 10^{23} \text{ kg})} = 9.24 \times 10^{-13} \text{ s}^2/\text{m}^3$$

$T = 1 \text{ day} = 24(3600 \text{ s}) = 86400 \text{ s}$ (synchronous satellite).

From $T^2 = Kr^3$, $r = \sqrt[3]{\frac{T^2}{K_M}} = \sqrt[3]{\frac{(86400 \text{ s})^2}{9.24 \times 10^{-13} \text{ s}^2/\text{m}^3}} = \boxed{2.0 \times 10^7 \text{ m}}$.

102. $T = 48 \text{ h} = (48 \text{ h})(3600 \text{ s/h}) = 1.728 \times 10^5 \text{ s}$. $r = 550 \text{ km} + 1500 \text{ km} = 2050 \text{ km} = 2.05 \times 10^6 \text{ m}$.

From Kepler's third law, $T^2 = \left(\frac{4\pi^2}{GM}\right)r^3$,

$$M = \frac{4\pi^2 r^3}{GT^2} = \frac{4\pi^2 (2.05 \times 10^6 \text{ m})^3}{(6.67 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2)(1.728 \times 10^5 \text{ s})^2} = \boxed{1.7 \times 10^{20} \text{ kg}}$$