

1. (a) The final velocity is equal in magnitude but opposite in direction to the initial velocity.

$$\Delta p = m\Delta v = m(v - v_o) = m(-v_o - v_o) = -2mv_o = -2(120 \text{ lb}) \times \frac{1 \text{ kg}}{2.2 \text{ lb}} \times (4.50 \text{ m/s})$$

$$= -491 \text{ kg}\cdot\text{m/s} = \boxed{491 \text{ kg}\cdot\text{m/s downward}}.$$

- (b) **Yes**, there would be a difference.

$$v^2 = v_o^2 - 2gy = (4.50 \text{ m/s})^2 - 2(9.80 \text{ m/s}^2)(-0.300 \text{ m}) = 26.13 \text{ m}^2/\text{s}^2, \quad \Rightarrow \quad v = -5.11 \text{ m/s}.$$

$$\text{So } \Delta p = (120 \text{ lb}) \times \frac{1 \text{ kg}}{2.2 \text{ lb}} \times (-5.11 \text{ m/s} - 4.50 \text{ m/s}) = -524 \text{ kg}\cdot\text{m/s} = \boxed{524 \text{ kg}\cdot\text{m/s downward}}.$$

2. (a) Apply momentum conservation $\vec{P}_o = \vec{P}$

$$\text{in } x\text{-axis: } (0.010 \text{ kg})(2000 \text{ m/s}) + 0 = (0.010 \text{ kg})(1000 \text{ m/s}) \cos 10^\circ + (100 \text{ kg}) v_{2x},$$

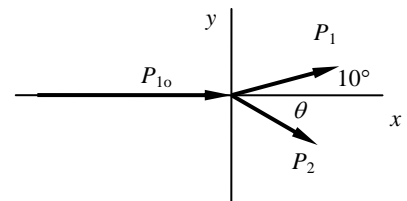
$$\text{so } v_{2x} = 0.1015 \text{ m/s};$$

$$\text{in } y\text{-axis: } 0 + 0 = (0.010 \text{ kg})(1000 \text{ m/s}) \sin 10^\circ + (100 \text{ kg}) v_{2y},$$

$$\text{so } v_{2y} = -0.01736 \text{ m/s}.$$

$$\theta_2 = \tan^{-1}\left(\frac{-0.01736}{0.1015}\right) = \boxed{9.7^\circ} \text{ below the } +x\text{-axis}.$$

$$(b) v_2 = \sqrt{(0.1015 \text{ m/s})^2 + (-0.0174 \text{ m/s})^2} = \boxed{0.10 \text{ m/s}}.$$



3. First consider the collision between car 1 and 2.

$$v_1 = \frac{m_1 - m_2}{m_1 + m_2} v_{1o} = \frac{2000 \text{ kg} - 1500 \text{ kg}}{2000 \text{ kg} + 1500 \text{ kg}} \times (15.0 \text{ m/s}) = \boxed{2.14 \text{ m/s}}.$$

$$v_2 = \frac{2m_1}{m_1 + m_2} v_{1o} = \frac{2(2000 \text{ kg})}{2000 \text{ kg} + 1500 \text{ kg}} \times (15.0 \text{ m/s}) = \boxed{17.1 \text{ m/s}}.$$

Now consider the collision between car 2 and 3.

The 17.1 m/s becomes the initial velocity in this collision. $v_2 = v_3 = v$.

$$(1500 \text{ kg})(17.1 \text{ m/s}) + (2500 \text{ kg})(0) = (1500 \text{ kg} + 2500 \text{ kg}) v, \quad \Rightarrow \quad v = \boxed{6.41 \text{ m/s}}.$$

4. (a) $\vec{P}_o = \vec{P}$, $\Rightarrow m_1 v_{1o} + m_2 v_{2o} = m_1 v_1 + m_2 v_2$.

$$(0.0200 \text{ kg})(300 \text{ m/s}) + (1.000 \text{ kg})(0) = (0.0200 \text{ kg})(50.0 \text{ m/s}) + (1.000 \text{ kg}) v_2. \quad \text{So } v_2 = \boxed{5.00 \text{ m/s}}.$$

$$(b) K_o = \frac{1}{2} (0.0200 \text{ kg})(300 \text{ m/s})^2 + \frac{1}{2} (1.000 \text{ kg})(0)^2 = 900 \text{ J}.$$

$$K = \frac{1}{2} (0.0200 \text{ kg})(50.0 \text{ m/s})^2 + \frac{1}{2} (1.000 \text{ kg})(5.00 \text{ m/s})^2 = 37.5 \text{ J}.$$

$$\text{So the fraction of the total initial kinetic energy lost is } \frac{900 \text{ J} - 37.5 \text{ J}}{900 \text{ J}} = \boxed{95.8\%}.$$

5. (a) $v_1 = v_2 = v$ (forms a single object). Apply momentum conservation $\vec{P}_o = \vec{P}$

$$\text{in } x\text{-axis: } (50.0 \text{ kg})(5.00 \text{ m/s}) - (0.50 \text{ kg})(35.0 \text{ m/s}) \cos 30^\circ = (50.0 \text{ kg} + 0.50 \text{ kg}) v_x, \quad \text{so } v_x = 4.650 \text{ m/s};$$

$$\text{in } y\text{-axis: } 0 - (0.50 \text{ kg})(35.0 \text{ m/s}) \sin 30^\circ = (50.0 \text{ kg} + 0.50 \text{ kg}) v_y, \quad \text{so } v_y = -0.1733 \text{ m/s}.$$

$$\theta_2 = \tan^{-1}\left(\frac{-0.1733}{4.650}\right) = \boxed{2.13^\circ} \text{ below the } -x\text{-axis}. \quad v = \sqrt{(-0.1733 \text{ m/s})^2 + (4.650 \text{ m/s})^2} = \boxed{4.65 \text{ m/s}}.$$

$$(b) K_o = \frac{1}{2} (50.0 \text{ kg})(5.00 \text{ m/s})^2 + \frac{1}{2} (0.50 \text{ kg})(35.0 \text{ m/s})^2 = 931 \text{ J}.$$

$$K = \frac{1}{2} (50.0 \text{ kg} + 0.50 \text{ kg})(4.65 \text{ m/s})^2 = 546 \text{ J}. \quad \text{So the answer is } \boxed{K < K_o, \text{ inelastic}}.$$

