

MOMENTUM - PROBLEM SET 2

$$\begin{aligned} \textcircled{1} \quad F &= 8.00 \text{ N} \\ m &= 4.00 \text{ kg} \\ t &= 12.0 \text{ s} \end{aligned}$$

$$Ft = m\Delta v$$

$$\textcircled{A} \quad \Delta v = \frac{Ft}{m} = \frac{(8.00 \text{ N})(12.0 \text{ s})}{4.00 \text{ kg}} = 24 \text{ m/s} \quad [\Delta v = 24.0 \text{ m/s}]$$

$$\textcircled{B} \quad \Delta p = m\Delta v = (4.00 \text{ kg})(24 \text{ m/s}) = 96 \text{ kg m/s} \quad [\Delta p = 96.0 \text{ kg m/s}]$$

$$\begin{aligned} \textcircled{2} \quad m &= 420 \text{ kg} \\ t &= 72.0 \text{ s} \\ v_1 &= 11.00 \text{ m/s} \\ v_2 &= 38.0 \text{ m/s} \end{aligned}$$

$$\textcircled{A} \quad \Delta p = m\Delta v = 420 \text{ kg} (38.0 \text{ m/s} - 11.00 \text{ m/s}) = 11340 \text{ kg m/s}$$

$$\textcircled{B} \quad \Delta p = Ft \quad F = \frac{\Delta p}{t} = \frac{11340 \text{ kg m/s}}{72.0 \text{ s}} = 157.5 \text{ N} \quad \begin{array}{l} [\Delta p = 11340 \text{ kg m/s}] \\ [F = 157 \text{ N}] \end{array}$$

$$\begin{aligned} \textcircled{3} \quad F &= 2.56 \times 10^3 \text{ N} \\ M &= 1.50 \times 10^3 \text{ kg} \\ v_1 &= 0 \\ v_2 &= 3.00 \times 10^2 \text{ m/s} \end{aligned}$$

$$Ft = m\Delta v$$

$$t = \frac{m(v_2 - v_1)}{F} = \frac{(1500 \text{ kg})(300 \text{ m/s} - 0)}{2.56 \times 10^3 \text{ N}} = 175.8 \text{ s} \quad [t = 176 \text{ s}]$$

$$\begin{aligned} \textcircled{4} \quad W &= 16850 \text{ N} \\ F &= -720 \text{ N} \\ v_2 &= 0 \\ v_1 &= 18.0 \text{ m/s} \end{aligned}$$

$$\textcircled{A} \quad W = mg \quad m = \frac{W}{g} = \frac{16850 \text{ N}}{10 \text{ m/s}^2} = 1685.0 \text{ kg} \quad [m = 1685 \text{ kg}]$$

$$\textcircled{B} \quad P_1 = m v_1 = (1685 \text{ kg})(18.0 \text{ m/s}) = 30330 \text{ kg m/s} \quad [P_1 = 30330 \text{ kg m/s}]$$

$$\textcircled{C} \quad \Delta p = m\Delta v = (1685 \text{ kg})(0 - 18 \text{ m/s}) = -30330 \text{ kg m/s} \quad [\Delta p = -30330 \text{ kg m/s}]$$

$$\textcircled{D} \quad Ft = \Delta p \quad t = \frac{\Delta p}{F} = \frac{-30330 \text{ kg m/s}}{-720 \text{ N}} = 42.125 \text{ s} \quad [t = 42.1 \text{ s}]$$

$$\begin{aligned} \textcircled{5} \quad m &= 2.4 \times 10^4 \text{ kg} \\ F &= 2.1 \times 10^5 \text{ N} \\ v_1 &= 0 \\ t &= 18.0 \text{ s} \end{aligned}$$

$$Ft = m\Delta v = m(v_2 - v_1)$$

$$v_2 = \frac{Ft}{m} + v_1 = \frac{(2.1 \times 10^5 \text{ N})(18.0 \text{ s})}{2.4 \times 10^4 \text{ kg}} + 0 = 157.5 \text{ m/s} \quad [v_2 = 157 \text{ m/s}]$$

$$\textcircled{6} \quad P_1 + P_2 = P'_1 + P'_2$$

$$m_1 v_1 + m_2 v_2 = m_1 v'_1 + m_2 v'_2$$

$$(4 \text{ kg})(22 \text{ m/s}) + (15 \text{ kg})(12 \text{ m/s}) = (4 \text{ kg})(9 \text{ m/s}) + (15 \text{ kg})(v'_2)$$

$$v'_2 = 15.466 \text{ m/s}$$

$$[v'_2 = 15.5 \text{ m/s}]$$

$$\textcircled{7} \quad P_B + P_W = P'_{B+W}$$

$$m_B v_B + m_W v_W = m_{B+W} v'_{B+W}$$

$$(0.42 \text{ kg})(v_B) + (9.0 \text{ kg})(0) = (0.42 + 9 \text{ kg})(9.2 \text{ m/s})$$

$$v_B = 1980.6 \text{ m/s}$$

$$[v_B = 1980 \text{ m/s}]$$

MOMENTUM PROBLEM SET 2

⑧ $P_{m+B} = P_m' + P_B'$ $(M_m + M_B) \bar{v}_{m+B} = M_m \bar{v}_m' + M_B \bar{v}_B'$
 $(65\text{kg} + 12\text{kg})(6\text{m/s}) = (65\text{kg})(7.5\text{m/s}) + (12\text{kg})\bar{v}_B'$, $\bar{v}_B' = 2.125\text{m/s}$
 $\bar{v}_B' = -2.125\text{m/s}$

⑨ $P_B + P_w = P_B' + P_w'$ $M_B \bar{v}_B + M_w \bar{v}_w = M_B \bar{v}_B' + M_w \bar{v}_w'$
 $(0.038\text{kg})(495\text{m/s}) + (3.0\text{kg})(0) = (0.038\text{kg})(260\text{m/s}) + (3.0\text{kg})(\bar{v}_w')$
 $\bar{v}_w' = 2.976$ $\bar{v}_w' = 2.98\text{m/s}$

⑩ $P_1 + P_2 = P_1' + P_2'$ $M_1 \bar{v}_1 + M_2 \bar{v}_2 = M_1 \bar{v}_1' + M_2 \bar{v}_2'$
 $(0.32\text{kg})(0.27\text{m/s}) + (0.150\text{kg})(0.13\text{m/s}) = (0.32\text{kg})\bar{v}_1' + (0.150\text{kg})(0.24\text{m/s})$
 $\bar{v}_1' = 1.0325\text{m/s}$ $\bar{v}_1' = 1.03\text{m/s}$

⑪ IMPULSE = $F \Delta t$
 $(35.0\text{N})(0.21\text{s}) = 7.35\text{N}\cdot\text{s}$ $\text{IMPULSE} = 7.35\text{N}\cdot\text{s}$

⑫ $m = 0.30\text{kg}$
 $\bar{v}_1 = 5.8\text{m/s}$
 $\bar{v}_2 = -16\text{m/s}$
 $t = 2.3 \times 10^{-2}\text{s}$ $Ft = m \Delta v$
 $F = \frac{m(\bar{v}_2 - \bar{v}_1)}{t} = \frac{(0.30\text{kg})(-16\text{m/s} - 5.8\text{m/s})}{2.3 \times 10^{-2}\text{s}} = -284.3\text{N}$
 $F = 284\text{N IN THE FINAL VELOCITY DIRECTION}$

⑬ $m = 800\text{kg}$
 $\bar{v} = 95\text{km/hr} = \frac{95\text{km}}{\text{hr}} \cdot \frac{1000\text{m}}{1\text{km}} \cdot \frac{1\text{hr}}{3600\text{s}} = 26.39\text{m/s}$
(A) $P = m\bar{v} = (800\text{kg})(26.39\text{m/s}) = 2.111 \times 10^4 \text{Kgm/s}$ $P = 2.11 \times 10^4 \text{Kgm/s}$
(B) $P = m\bar{v} \quad \bar{v} = \frac{P}{m} = \frac{2.111 \times 10^4 \text{Kgm/s}}{2385\text{kg}}$
 $\bar{v} = 8.851\text{m/s}$ $\bar{v} = 31.9\text{km/hr}$
 $8.851\text{m/s} \cdot \frac{3600\text{s}}{1\text{hr}} \cdot \frac{1\text{km}}{1000\text{m}} = 31.86\text{km/hr}$

⑭ $m = 550\text{kg}$ (A) $\Delta P = m \Delta v = m(\bar{v}_2 - \bar{v}_1) = (550\text{kg})(38.0 - 8.0\text{m/s}) = 16500\text{Kgm/s}$
 $\bar{v}_1 = 8.0\text{m/s}$ $\Delta P = 16500\text{Kgm/s}$
 $\bar{v}_2 = 38.0\text{m/s}$
 $t = 62.0\text{s}$ (B) $\Delta P = F t \quad F = \frac{\Delta P}{t} = \frac{16500\text{Kgm/s}}{62.0\text{s}} = 266.1\text{N}$
 $F = 266\text{N}$